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A Multi-State Model of the CaMKII Dodecamer Suggests a Role for Calmodulin in Maintenance of Autophosphorylation

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Abstract

Ca^{2+} /calmodulin-dependent protein kinase II (CaMKII) accounts for up to 2 percent of all brain protein and is essential to memory function. CaMKII activity is known to regulate dynamic shifts in the size and signaling strength of neuronal connections, a process known as synaptic plasticity. Increasingly, computational models are used to explore synaptic plasticity and the mechanisms regulating CaMKII activity. Conventional modeling approaches may exclude biophysical detail due to the impractical number of state combinations that arise when explicitly monitoring the conformational changes, ligand binding, and phosphorylation events that occur on each of the CaMKII holoenzyme's subunits. To manage the combinatorial explosion without necessitating bias or loss in biological accuracy, we use a specialized syntax in the software MCell to create a rule-based model of a twelve-subunit CaMKII holoenzyme. Here we validate the rule-based model against previous experimental measures of CaMKII activity and investigate molecular mechanisms of CaMKII regulation. Specifically, we explore how Ca^{2+} /CaM-binding may both stabilize CaMKII subunit activation and regulate maintenance of CaMKII autophosphorylation. Noting that Ca^{2+} /CaM and protein phosphatases bind CaMKII at nearby or overlapping sites, we compare model scenarios in which Ca^{2+} /CaM and protein phosphatase do or do not structurally exclude each other's binding to CaMKII. Our results suggest a functional mechanism for the so-called "CaM trapping" phenomenon, wherein Ca^{2+} /CaM may structurally exclude phosphatase binding and thereby prolong CaMKII autophosphorylation. We conclude that structural protection of autophosphorylated CaMKII by Ca^{2+} /CaM may be an important mechanism for regulation of synaptic plasticity.

Author summary

In the hippocampus, dynamic fluctuation of the size and strength of neuronal connections is thought to underlie learning and memory processes. These fluctuations, called synaptic plasticity, are in part regulated by the protein calcium/calmodulin-dependent kinase II (CaMKII). During synaptic plasticity, CaMKII becomes activated in the presence of calcium ions (Ca^{2+}) and calmodulin (CaM), allowing it to interact enzymatically with downstream binding partners. Interestingly, activated CaMKII can phosphorylate itself, resulting in state changes that allow CaMKII to be functionally active independent of Ca^{2+} /CaM. Phosphorylation of CaMKII at Thr-286/287 has been shown to be a critical component of learning and memory. To explore the molecular mechanisms that regulate the activity of CaMKII holoenzymes, we use a rule-based approach that reduces computational complexity normally associated with representing the wide variety of functional states that a CaMKII holoenzyme can adopt. Using this approach we observe regulatory mechanisms that might be obscured by reductive approaches. Our results suggest that CaMKII phosphorylation at Thr-286/287 may be stabilized by a mechanism in which CaM structurally excludes phosphatase binding at that site.

Introduction

CaMKII is a protein of interest because of its crucial role in synaptic plasticity [1-5]. In the hippocampus, synaptic plasticity in the post-synapse occurs within mushroom-shaped protrusions called dendritic spines [6]. Synaptic plasticity is dependent on calcium ion (Ca^{2+}) flux through N-methyl-D-aspartate receptors (NMDARs) located on the dendritic spines of the post-synaptic neuron [7]. Depending on the magnitude, frequency, and location of Ca^{2+} flux, synaptic plasticity may produce increases or decreases (or neither) in synaptic strength [8, 9]. Large, higher-frequency Ca^{2+} spikes can induce an enduring up-regulation of synaptic strength, called long-term potentiation (LTP); while weak, lower-frequency Ca^{2+} spikes can induce an enduring down-regulation of synaptic strength, called long-term depression (LTD) [9, 10]. Whether Ca^{2+} spikes induce LTP or LTD depends on relative activation of intracellular protein signaling networks. When Ca^{2+} first enters the dendritic spine, it interacts with a

variety of buffer and sensor proteins, chiefly calmodulin (CaM), which has many protein targets in the spine, including CaMKII [5, 11, 12].

The CaMKII holoenzyme contains at least twelve subunits [13-16] arranged as two rings of six. As shown in Fig 1, each CaMKII subunit features an N-terminal kinase domain and C-terminal hub domain [17]. Between the kinase and hub domains is a flexible regulatory domain which lends to the subunit a wide range of movement away from the holoenzyme's central hub. A crystal structure of human alpha-CaMKII expressed in *E. coli* published by Chao *et al.* (2011) shows CaMKII subunits as able to rapidly and stochastically pivot between a “docked” and “undocked” conformation, seemingly mediated by residues on the kinase domain's activation loop and a spur structure on the hub domain (see Fig 3C in [17]), such that a docked subunit may be inaccessible to CaM binding. In contrast, a more recent work using electron microscopy with rat alpha-CaMKII expressed in Sf9 cells suggests that less than 3 percent of subunits exhibit a compact (or docked) conformation [18]. Given the uncertainty in the field, we include subunit docking and undocking in our model, allowing for future exploration of this possible subunit functionality. In addition to docking and undocking, each subunit can be in an “inactive” conformation when the regulatory domain is bound to the kinase domain (Fig 1B), or an “active” conformation when this binding is disrupted by thermodynamic effects. In this work, we describe CaMKII subunit activation as highly transient until stabilized by a fully-bound Ca^{2+} /CaM or phosphorylation at Thr-286 [17, 19]. In the active conformation the catalytic domain of a subunit is able to bind and phosphorylate enzymatic substrates. A subunit may spontaneously return to an inactive conformation in the absence of Ca^{2+} /CaM or phosphorylation at Thr-286 [19].

Fig 1. Schematic of CaMKII Subunit Structure. (A) Map of amino acid residues in a CaMKII subunit. The N-terminal kinase domain (blue) approximately spans residues 1-274. The regulatory domain (residues 275-314, yellow) binds to the kinase domain autoinhibiting the kinase activity of the each CaMKII subunit. The putative phosphatase binding site is also shown purple. The Ca^{2+} /CaM binding site is shown in orange. Subunits self-associate via the hub domain (residues 315-475, green) to form multimeric complexes of 12-14 subunit holoenzymes. (B) The “inactive” CaMKII subunit (derived from a crystal structure found on the Protein Data Bank, or PDB, entry code 3SOA) in which the regulatory domain (yellow) is closely associated with the kinase domain (blue). (C) A schematic of the “active” CaMKII subunit. The regulatory domain (yellow) swings away from the kinase domain (blue). This

schematic was generated by manually modifying PDB entry 3SOA to illustrate how the regulatory domain may be available for Ca^{2+} /CaM binding and the kinase domain open for substrate binding. (D) Cartoon depiction of all protein species in our model, in which Ca^{2+} /CaM (orange) or phosphatase (purple) may bind to the regulatory domain (yellow) of a CaMKII subunit.

CaMKII can become enzymatically active in the absence of Ca^{2+} /CaM-binding via phosphorylation at Thr-286, which is required for LTP [3, 20]. Importantly, this phenomenon is an autophosphorylation: it is thought to occur when an active subunit phosphorylates neighboring subunits within the same holoenzyme [21, 22]. Autophosphorylation at Thr-286 (“pThr-286”) is thought to provide structural stability to a subunit’s active conformation (reviewed in [23]) [24]. Because CaMKII plays a key role in the induction of LTP, and ultimately learning and memory (reviewed in [4, 8]), we seek to better understand the biochemical regulation of CaMKII activation and autophosphorylation via computational modeling.

To characterize the spatiotemporal regulation of CaMKII, experimental studies are increasingly complemented by computational models [15, 17, 25-28]. Computational models of Ca^{2+} -dependent signaling implicate competition, binding kinetics, feedback loops, and spatial effects in regulating enzyme activation [7, 12, 24, 29, 30]. However, fully characterizing these and other mechanisms of CaMKII regulation is impeded by the challenge of accurately portraying the CaMKII holoenzyme. As described by previous work, combinatorial explosion can occur when modeling CaMKII (and similar biomolecules) activation because the protein exhibits a large number of functionally significant and not necessarily inter-dependent states [24, 26, 31-33]. The large number of possible states of CaMKII can neither be explicitly specified nor efficiently evaluated with conventional mass action-based methods. Indeed, for just one CaMKII hexamer ring, we estimate a state space of ~32 billion states, and for the full dodecamer approximately 10^{20} possible states (See S1 Appendix). The numbers of possible CaMKII states far exceeds the number of CaMKII molecules in a dendritic spine, suggesting that some states rarely occur and thus likely contribute little to protein function. Previous models leverage this observation to reduce the model state space and provide valuable insight to CaMKII binding and autophosphorylation dynamics [24, 33-36]. However, for CaMKII it remains unclear which states functionally participate in synaptic

plasticity. Reduced models can inadvertently obscure key mechanisms regulating CaMKII activation and autophosphorylation. To elucidate complex regulatory mechanisms, it may be necessary for models to provide for all possible states *ab initio*.

In this work, we use rule-based model specification and particle-based rule evaluation methods to overcome combinatorial explosion [26, 32, 37]. Rules are conditions, based primarily on experimental observations, that prescribe when an implicitly-defined reaction may occur. At a given iteration, only states that matter for the execution of a particular rule are explicitly declared. States that do not matter to a particular rule can be omitted, a principle that has been paraphrased as “don’t care, don’t write” [38]. We use rule- and particle-based methods within the spatial-stochastic software MCell 3.3 [30, 39] to present a comprehensive multi-state model of the CaMKII dodecamer. Other simulation platforms can also overcome combinatorial explosion through rule-based model specification (e.g. BioNetGen [40]) or network-free approaches (e.g. NFsim [41]). Unlike other platforms, MCell 3.3 provides both spatial-stochastic and rule-based modeling, although multi-state molecules in MCell 3.3 cannot diffuse. We use MCell 3.3 in anticipation of future MCell versions accounting for multi-state molecule diffusion, and to eventually build on simulations with physiological dendritic spine geometries such as those by Bartol *et al.* (2015) [42].

Here, we validate this rule-based MCell model of CaMKII regulation against current descriptions of the Ca^{2+} frequency-dependence of CaMKII activation. By varying the rules and model parameter values we can simulate different experimental manipulations of CaMKII interaction with Ca^{2+} /CaM and phosphatase and thereby explore various mechanisms regulating CaMKII activity. In particular, we show that Ca^{2+} /CaM is important not only for regulating activation of CaMKII but may also contribute to the maintenance of CaMKII phosphorylation at Thr-286. We hypothesize that by limiting access of phosphatases to CaMKII Thr-286 (perhaps by steric hindrance), Ca^{2+} /CaM may prolong the lifetime of the auto-phosphorylated state.

Results

Model Development

Molecular Species. The model contains three protein species: CaM, protein phosphatase, and CaMKII.

Ca²⁺/CaM facilitates CaMKII activation, which leads to autophosphorylation at Thr-286, and phosphatase activity facilitates de-phosphorylation at Thr-286. Both protein phosphatase 1 (PP1) and protein phosphatase 2A (PP2A) have been shown to dephosphorylate Thr-286, though in different subcellular fractions (reviewed by [21, 43-45]). Here we refer to them generally as protein phosphatase (PP).

CaM and PP are modeled in MCell as conventional cytosolic molecules. Initially, CaM is modeled as having one of two states: un-bound apo-CaM which does not bind CaMKII, and fully-saturated Ca²⁺/CaM (four Ca²⁺ bound to CaM) which does bind CaMKII similar to previous studies [29, 46]. Notably, we and others have described the importance of sub-saturated Ca²⁺/CaM states with fewer than 4 Ca²⁺ [12, 24, 33, 47-49]. Thus, we also explore the dynamics of Ca²⁺-CaM binding and the binding of sub-saturated Ca²⁺/CaM to CaMKII. However, accounting for sub-saturated Ca²⁺/CaM would here require a multi-state representation, and because multi-state molecules cannot diffuse in MCell 3.3, we simplify our Ca²⁺/CaM model to allow CaM to diffuse and interact with a (non-diffusing) multi-state representation of CaMKII. PP is modeled as single-state protein that is constitutively active and able to bind auto-phosphorylated CaMKII subunits. Our representation of constitutively active PP is consistent with previous models such as that by Lisman and Zhabotinsky (2001) [50].

CaMKII is modeled as a multi-subunit, multi-state complex, defined using a specialized model syntax for complex molecules (COMPLEX_MOLECULE) in MCell 3.3 [51]. This syntax allows for explicit representation of individual CaMKII dodecamers with distinguishable subunits. As shown in Fig 2, the holoenzyme is arranged as two directly-apposed, radially-symmetric rings each with six subunits. Each subunit can independently undergo state changes (e.g. subunit docking/undocking, CaM binding, phosphorylation at Thr-298, phosphorylation at Thr-306, binding to PP, see Fig 2). Each of these subunit state changes are represented as five “flags”, each standing for a particular state that each CaMKII subunit can adopt. Note that all states are not mutually exclusive (i.e. a subunit can be phosphorylated at Thr-286

and bound to CaM simultaneously). Flags are used in rule evaluation, which occurs at each time step and for each individual subunit. That is, MCell repeatedly evaluates model rules against a given subunit's flags (and those of the neighboring subunits) to determine which state transitions a subunit undertakes at each time step. In the following sub-sections, we describe all CaMKII model flags, the state transitions that apply to each flag, the conditions and rate parameters for each state transition, and related model assumptions. In Fig 2, we visually convey how CaMKII subunits transition between states according to the model's rules. We summarize the state transition rules and rate parameter values in Table S1.

Fig 2. CaMKII holoenzyme state transitions. (A) Our model of CaMKII has twelve individual subunits arranged in two radially symmetric, directly apposed rings. Subunits may spontaneously undock/extend from the central hub or dock/retract (if inactive). Whether docked or undocked, subunits may spontaneously open/activate. (B) If two neighboring subunits are active, one may auto-phosphorylate the other at Thr-286. If auto-phosphorylated (pThr-286), a subunit may remain active even upon un-binding of CaM. A pThr-286 subunit un-bound to CaM may additionally phosphorylate at Thr-306, blocking subsequent re-binding of Ca^{2+} /CaM. A pThr-286 subunit may also bind and become de-phosphorylated by PP (purple).

Flag 1: Subunit docking. Docking is a binary flag that describes CaMKII kinase subunits as either “docked” or “undocked” to the CaMKII central hub. Subunits are instantiated in a docked state but may undergo numerous transitions between docked and undocked over the course of a simulation. At each time step, we assess a rule governing the subunit's transition from a docked to undocked state (see S1 Appendix Table S1). If this rule is satisfied, meaning that the subunit's docking flag is verified as “docked”, then the transition to “undocked” is considered. Similarly, we assess a separate rule governing a transition from an undocked to docked state, which requires that the subunit not be bound to CaM and not phosphorylated at Thr-306 [17].

Subunit docking follows the structural model of Chao *et al.*, who showed that a subunit cannot bind CaM as long as the subunit is in a compact conformation, docked to its central hub [17]. Docking implies a two-step process in which the subunit must first un-dock before subsequent CaM-binding, which accounts for the reported difference in binding rate for CaM to CaMKII-derived peptide (1×10^8

M⁻¹s⁻¹ [52]) and for CaM to full-length CaMKII-T286A (1.8×10^6 M⁻¹s⁻¹ [53]). Taking the ratio of these two rates gives an equilibrium constant for docking of 0.018, which is consistent with estimates by Chao *et al.*, who assumed K_{docking} to fall between 0.01 and 100 [17]. With this equilibrium constant, we estimate kinetic rates for docking and undocking. For this estimation, we first note that subunit docking involves a structural conformation change on a relatively large scale. Referring to a separate, and notably smaller-scale, conformational change in our model, in which CaM quickly transitions from an initially- to fully-bound state (see Flag 3: CaM Binding), we assume the docked-to-undocked transition to proceed at an order of magnitude slower. We therefore arrive at an assumed rate for k_{dock} of 35 s⁻¹. In turn, this gives an undocking rate $k_{\text{undock}} = k_{\text{dock}} \times K_{\text{docking}}$ of 0.63 s⁻¹, which lies within the range of 0.01 s⁻¹ and 100 s⁻¹ for k_{undock} assumed by Chao *et al.*

Flag 2: Subunit activation. The activation flag describes CaMKII subunits as either “active” or “inactive”. An inactive subunit has no catalytic activity because the regulatory domain is bound to the subunit’s catalytic site. Conversely, an active subunit has catalytic activity because the regulatory domain’s inhibition of the kinase domain is disrupted. When a subunit is active, Ca²⁺/CaM and/or other proteins may access and bind CaMKII. In our model, the transition reaction from inactive to active involves no explicit rules (but rather occurs unconditionally and as governed by rates described below). In contrast, two rules inform the conditions for subunit inactivation: that the subunit is 1) not fully-bound to CaM, and 2) not phosphorylated at Thr-286.

To assign rate parameters for this flag, we first note that subunits can fluctuate between inactive and active states rapidly in the absence of Ca²⁺/CaM (on the order of hundreds of nanoseconds) [19, 54]. Noting this, we set the rate parameter for subunit inactivation at 1×10^7 s⁻¹. Further, Stefan *et al.* determined that the activation probability (in the absence of CaM and phosphorylation) is 0.002, leading us to set our activation rate parameter to 2×10^4 s⁻¹ [31]. Thus, we arrive at a model in which CaMKII subunit activation is unstable until stabilized by CaM-binding or autophosphorylation.

Flag 3: CaM binding. CaM binding is a ternary flag meaning that each CaMKII subunit displays one of three states, where CaM may be “unbound”, “initially-bound”, or “fully bound”. We emphasize that until we present a so-called “9-state-1-step” model of CaM-CaMKII (see the end of Results), in this paper “CaM” generally refers to fully-saturated $\text{Ca}^{2+}/\text{CaM}$ (or CaM_4) bound to CaMKII. Our model adapts previous work by Stefan *et al.* (2012) to describe CaM-binding to CaMKII as a two-step process [31]. First, CaM binds to the regulatory domain of a CaMKII subunit (residues 298-312), resulting in a low-affinity “initially bound” CaMKII state, which is compatible with both the inactive (closed) and active (open) subunit conformation. Second, if the initially bound CaMKII opens it may transition to a “fully bound” state that describes the complete, higher-affinity interaction between CaM and CaMKII along residues 291-312 (see Figure 5 in [31]). The transition from an unbound to initially bound state requires the subunit must be: 1) undocked, 2) not PP-bound, and 3) un-phosphorylated at Thr-306. The transition reaction from initially bound to a fully bound state requires just that the subunit already be active/open. Dissociation of CaM from a fully bound CaM-CaMKII state proceeds through the initially bound state before becoming completely unbound from CaMKII.

In order to determine the parameters governing initial binding of CaM to CaMKII, we use data on CaM binding to CaMKII-derived peptides, rather than full-length CaMKII. This is done to separate the intrinsic binding constants from the parameters governing subunit activation/inactivation and docking/undocking. We use the microscopic k_{on} for CaM binding to CaMKII measured by [52], using a CaMKII peptide and fluorescently labeled DA-CaM, as $1 \times 10^8 \text{ M}^{-1}\text{s}^{-1}$. For the K_D governing initial CaM binding, we use the K_D reported by Tse *et al.* for CaM binding to a low-affinity peptide (CaMKII residues 300-312), which is $5.9 \times 10^{-6} \text{ M}$ [55]. From these two parameters, we can compute the dissociation rate of initially-bound CaM from CaMKII: $k_{\text{off_CaM_ini}} = K_{\text{d_CaM_ini}} \times k_{\text{on_CaM}} = 590 \text{ s}^{-1}$. While this rate may seem fast, we emphasize that in our model CaM dissociation happens in two steps, with the transition from fully-bound to initially-bound CaM which we discuss next.

In order to determine the parameters governing the transition from initially-bound to fully-bound CaM to CaMKII, we note that this transition involves a structural compaction of the CaM molecule, which has been measured using fluorescent labels [52, 53]. Using fluorescent labels to analyze the structural compaction of CaM is convenient in its exclusion of effects due to conformational changes within CaMKII subunits or the CaMKII holoenzyme. Thus, we use these measurements as a proxy for CaM binding to a CaMKII peptide and to estimate parameters governing the transition between initially- and fully-bound CaM-CaMKII. Taken from experimental measurements by Torok *et al.*, we identify a transition rate from initially-bound to fully-bound CaM-CaMKII (compaction of CaM) of 350 s^{-1} and from fully-bound back to initially-bound CaM-CaMKII (de-compaction of CaM) of $4 \times 10^{-3} \text{ s}^{-1}$ [52]. This means that, in the absence of obstructions to binding, the likelihood of a bound CaM molecule being in the initial binding state (rather than the fully bound state) is $4 \times 10^{-3} / 350 = \sim 1.1 \times 10^{-5}$. This is consistent with a probability of CaM being bound to the high-affinity site of 0.99999 which was derived by Stefan *et al.* (2012) [31].

Flag 4: Phosphorylation at Thr-286. Phosphorylation at the residue Thr-286 is a ternary flag that describes this site as either “un-phosphorylated (uThr-286)”, “phosphorylated (pThr-286)”, or “phosphatase-bound”. We specify four rules to govern the reaction that transitions a subunit from uThr-286 to pThr-286: the subunit 1) be uThr-286, 2) be undocked, 3) be active, and 4) have an active and undocked neighbor subunit in the same holoenzyme ring. Notably, we do not require that a subunit be CaM-bound for autophosphorylation to occur; however, because an un-bound CaMKII subunit’s activation is highly transient, we find that CaM-binding is effectively required for autophosphorylation at Thr-286 (shown in Model Validation). Similarly, because pThr-306 (discussed in Flag 5) prohibits CaM-binding, we find that autophosphorylation at Thr-286 effectively requires uThr-306, though we do not explicitly state this rule. The neighboring subunit’s activation flag is considered because autophosphorylation is facilitated by its catalytic site. Our model only considers the counter-clockwise neighbor subunit because, in the absence of experimental observations to the contrary, we assume that

steric effects cause autophosphorylation to occur in only one direction about a CaMKII ring, similar to previous work [56, 57]. The rate of autophosphorylation, 1 s^{-1} , at Thr-286 is taken from an earlier study of CaMKII autophosphorylation in the presence of CaM [47].

De-phosphorylation of pThr-286 is facilitated by binding and enzymatic activity of protein phosphatases PP1 and PP2A, here referred to generally as PP [43, 44]. Two rules govern PP binding to a CaMKII subunit (the transition from pThr-286 to a phosphatase-bound state): that the subunit be 1) phosphorylated at Thr-286 (pThr-286) and 2) not be bound to CaM. It has been shown that a majority of autophosphorylated CaMKII in the PSD is dephosphorylated by PP1 [58, 59]; while in brain extracts autophosphorylated CaMKII is mostly dephosphorylated by PP2A [43]. The requirement that CaM be unbound from CaMKII in order for PP to bind to CaMKII is motivated by the observation that simultaneous binding of CaM and PP to the CaMKII regulatory domain may be mutually exclusive due to steric hindrance. CaM, having molecular weight 18 kDa, binds to the CaMKII regulatory domain around residues 290–309 [56, 60, 61], which is at least 4 residues, and at most 23 residues away from Thr-286 (again, see also Figure 5 in [31]). To the best of our knowledge, the peptide binding footprint of neither PP (PP1 nor PP2A) onto CaMKII is fully described. However, both PP1 and PP2A are widely known to target pThr-286 [58, 59, 62] and de-phosphorylate threonine residues nearby alpha helices in other substrates [63, 64]. Additionally, the catalytic subunit of PP1 has a molecular weight of 37 kDa, which is nearly twice that of CaM and more than half that of a CaMKII subunit. Taken together, we hypothesize that the PP binding footprint likely overlaps with the CaM binding site, such that the presence of bound PP likely structurally excludes or impedes upon a subsequent binding of CaM to CaMKII. Similarly, the presence of bound Ca^{2+} /CaM structurally would exclude coincident binding of PP. In S1 Appendix, we further discuss the quantitative basis of this structural exclusion hypothesis in light of the crystal structure of the PP1-spinophilin interaction (PDB: 3EGG) [65]. In short, PP1 tends to bind substrates at a site $>20\text{\AA}$ from the PP1 active site. Thus, if the PP1 binding footprint does not actually contain T286, then the furthest likely CaMKII residue of PP1 binding (at least on the hub domain side of T286) is G301, well

within the CaM binding footprint (S1 Appendix). We examine the regulatory implications of this hypothesis by relaxing the rules of PP binding and requiring only that the subunit be pThr-286. The kinetic rates of PP binding CaMKII are based on values used by Zhabotinsky (2000), using the same catalytic rate of 2 s^{-1} and choosing values for the association ($3 \times 10^6 \text{ M}^{-1} \text{ s}^{-1}$) and dissociation (0.5 s^{-1}) rate constants such that the resulting Michaelis constant ($8.3 \times 10^{-7} \text{ M}$) falls in the range used by Zhabotinsky [46].

Flag 5: Phosphorylation at Thr-306. Phosphorylation at the residue Thr-306 is a binary flag that describes this site as either un-phosphorylated (“uThr-306”) or phosphorylated (“pThr-306”). We model the transition from uThr-306 to pThr-306 using three rules: that the subunit be 1) uThr-306, 2) active, and 3) un-bound by CaM. Our model uses a forward rate parameter 50-fold slower than that of phosphorylation at Thr-286, based on past experimental measurements [35, 66]. Over the course of our simulation times, we observe very few pThr-306 transitions and therefore exclude the reverse transition reaction describing de-phosphorylation of pThr-306 into uThr-306. Notably, we do not require that a subunit be pThr-286 as a condition for becoming pThr-306. However, because a subunit’s activation is highly transient when un-bound by CaM in our model, the probability of pThr-306 acquisition is quite small if the subunit is not already pThr-286.

Model Validation

Stimulation frequency correlates with subunit activity

To validate our model, we assessed a variety of model outputs under various regimes of $\text{Ca}^{2+}/\text{CaM}$ stimulation. As a first assessment, we simulated a persistent $\text{Ca}^{2+}/\text{CaM}$ bolus (note that here we only use the fully saturated CaM_4 as the active form of $\text{Ca}^{2+}/\text{CaM}$), similar to experiments by Bradshaw *et al.* (2002), who monitored CaMKII autophosphorylation over time [57]. In Fig 3 we simultaneously monitored the time-course concentration of CaMKII subunit flags indicating: initially-bound $\text{Ca}^{2+}/\text{CaM}$, fully-bound $\text{Ca}^{2+}/\text{CaM}$, active CaMKII, and pThr-286 (Fig 3). In the persistent, continuous presence of $\text{Ca}^{2+}/\text{CaM}$, the concentration of subunits with initially-bound $\text{Ca}^{2+}/\text{CaM}$ (yellow trace) is noisy and

consistently low, implying that initially-bound $\text{Ca}^{2+}/\text{CaM}$ seems rapidly to either dissociate or proceed to a fully-bound conformation. Fully-bound $\text{Ca}^{2+}/\text{CaM}$ (red trace) subunit concentrations closely follow those of active CaMKII subunits (dark blue trace) over time, providing evidence that $\text{Ca}^{2+}/\text{CaM}$ stabilizes CaMKII activation. Indeed, because the difference in concentrations of fully-bound $\text{Ca}^{2+}/\text{CaM}$ and active CaMKII is always small, we observe that although unbound CaMKII may spontaneously activate, these activated subunits rapidly return to an inactive state and are not likely to progress to a phosphorylated (pThr-286) state. We next observe that the increase of CaMKII autophosphorylation at Thr-286 (cyan trace) over time is strongly associated with increases in the number of subunits that are fully-bound to $\text{Ca}^{2+}/\text{CaM}$ and active subunits (dark blue and red traces, respectively). This is consistent with previous work showing that $\text{Ca}^{2+}/\text{CaM}$ must be bound to CaMKII for pThr-286 to occur [56] and CaMKII Ca^{2+} -independent activity is strongly associated CaMKII autophosphorylation at Thr-286 [17, 53, 67, 68]. Furthermore, we observe in Fig 3A that more than 80 percent of CaMKII subunits are autophosphorylated at $t=20\text{sec}$, which is of similar magnitude and timescale as observed by Bradshaw *et al.* (see Figure 2A in [57]).

Fig 3. Validation of the Rule-based Model. Bold traces (A-C) and solid circles (D) are the average of $N = 50$ executions. For each species (A-C), six representative traces are also shown (semi-transparent lines). (A) Model output resulting from stimulation with a large continuous bolus of $\text{Ca}^{2+}/\text{CaM}$. Concentrations of active (red), initially CaM-bound (yellow), fully CaM-bound (blue), and pThr-286 (cyan) subunits. (B) Time-course average concentration (bold trace) of active subunits stimulated by 5 Hz or 50 Hz $\text{Ca}^{2+}/\text{CaM}$. (C) Time-course concentration of pThr-286 subunits stimulated continuously by 5 Hz or 50 Hz $\text{Ca}^{2+}/\text{CaM}$. (D) Frequency-dependent activation (red) and pThr-286 (cyan) of CaMKII subunits, with SEM error bars. Black dotted traces are linear fits.

Next, we assessed model behavior under low- and high-frequency stimulating conditions. CaMKII activation and autophosphorylation at Thr-286 in response to 5Hz and 50Hz $\text{Ca}^{2+}/\text{CaM}$ is plotted in Figure 3B and 3C, respectively; 50 seeds were run for each condition, with 6 representative traces (transparent lines) and the average response (bold) plotted. As expected, the data showed significantly greater levels of CaMKII activation and autophosphorylation at 50Hz relative to 5Hz stimulation [12, 20]. Indeed, our results in Fig 3C are comparable to results from Shifman *et al.* (2006), who observed much

lower autophosphorylation at low $\text{Ca}^{2+}/\text{CaM}$ concentrations (less than 2 μM) than at high concentrations (see Figure 4D in [47]).

To further determine how stimulation frequency affects CaMKII activity, the model was stimulated continuously at frequencies ranging from 1Hz to 50 Hz. The concentrations of the various CaMKII states $t=20$ seconds of simulation time are plotted as a function of frequency in Fig 3D. We observe a nearly linear correlation between both subunit activation ($R^2 = 0.99$) and pThr-286 ($R^2 = 0.96$). This is consistent with computational results from Chao *et al.*, who developed a stochastic model that also yielded a linear relationship between pThr-286 and stimulation frequency for frequencies greater than 1 Hz [15]. Additionally, our results in Fig 3D show that the model elicits $\sim 5\%$ ($\sim 1\mu\text{M}$ out of $18.24\mu\text{M}$ total) CaMKII pThr-286 in response to 10Hz stimulation (Fig 3D), which is in general agreement with experimental results given our relatively short pulse width of 10msec (see Figure 4A in [69]). In S1 Appendix, we further simulate our model for 20sec at 4Hz $\text{Ca}^{2+}/\text{CaM}$ using a pulse width of 200msec, yielding $\sim 50\%$ pThr-286, consistent with [69] (see Figure 3B in that paper). Taken together, these results (Fig 3 and Figure S1) show that our model behaves as expected and is able to produce CaMKII activity and autophosphorylation behaviors similar to previous computational and experimental results.

Exploring CaMKII Holoenzyme Phosphorylation

A Thresholded Response of CaMKII to $\text{Ca}^{2+}/\text{CaM}$

CaMKII has long been theorized to exhibit switch-like or bistable behavior, which could underlie the importance of pThr-286 to learning and memory formation [4, 46, 50, 70, 71]. However, experimental efforts have struggled to identify a bistability making CaMKII activity robust to the presence of phosphatases. Recently, Urakubo *et al.* used the chelator EGTA to control single pulses of Ca^{2+} in a mixture of CaM, CaMKII, PP1, and NMDAR peptides, leading to what seemed to be the first direct observation of CaMKII bistability in the presence of NMDAR peptides only [72]. Noting this, we explored whether a spatial stochastic model of the CaMKII dodecamer would exhibit switch-like behavior for concentration parameters of Ca^{2+} , CaM, CaMKII, and PP known to exist in hippocampal spines. We

stimulated the model with a set of short $\text{Ca}^{2+}/\text{CaM}$ input pulses (which could also be reproducible *in vitro*). Importantly, we did not aim to identify true bistability because exploring the many combinations of Ca^{2+} , kinase, and phosphatase concentrations was outside the scope of this paper. Instead we wondered if, by stimulating with brief pulses of $\text{Ca}^{2+}/\text{CaM}$ of variable duration, our model would exhibit switch-reminiscent pThr-286 behavior. Specifically, we hypothesized that there would exist a threshold of time of $\text{Ca}^{2+}/\text{CaM}$ below which pThr-286 was unachievable and above which pThr-286 was maintained. At stimulation durations above this threshold enough CaMKII autophosphorylation (pThr-286) would occur and self-propagate in balance with de-phosphorylation by PP.

In Fig 4 we exposed our model to single $\text{Ca}^{2+}/\text{CaM}$ pulses of constant magnitude but of variable duration (similar to Figure 1B in [72]). The model was stimulated with single $\text{Ca}^{2+}/\text{CaM}$ input pulses of magnitude 22.8 μM and varying duration (0.05, 0.1, 0.2, 0.3, 0.4, or 0.5 sec). Different pulse durations resulted in distinct levels of subunit activation, where longer pulse durations resulted in greater activation and autophosphorylation (p-Thr286) levels, (Fig 4A and B, respectively). Interestingly, subunits stimulated by even the shortest pulses of 0.05 or 0.1 sec, appeared to sustain their activation for the simulation period (120 sec). However, these short-pulse (0.05-0.1 sec) stimulations rarely resulted in autophosphorylation (pThr-286, Fig 4B). Longer (0.2-0.5 sec) $\text{Ca}^{2+}/\text{CaM}$ pulses resulted in greater levels of subunit activation that started declining immediately after the $\text{Ca}^{2+}/\text{CaM}$ pulse ended (Fig 4A), but elicited pThr-286 levels that were generally sustained for the duration of a simulation (Fig.4B). Taken together, we found that CaMKII may be thresholded at a level of $\text{Ca}^{2+}/\text{CaM}$ exposure below which pThr-286 is unobserved and above which pThr-286 is achieved and subsequently sustained across several minutes even in the presence of phosphatase.

Fig 4. Response to short $\text{Ca}^{2+}/\text{CaM}$ pulse stimulation. Average concentration of (A) active and (B) pThr-286 CaMKII subunits over time, following $\text{Ca}^{2+}/\text{CaM}$ stimulating pulses of length 0.05 (red), 0.1 (blue), 0.2 (green), 0.3 (purple), 0.4 (yellow), and 0.5 (orange) seconds. Each trace represents the average of N=50 executions. See Appendix S1 for identical data shown with SEM error bars and over the first two seconds of simulated time. As detailed in Methods, the CaM concentration is here 22.8 μM (450 particles).

We also explored how this $\text{Ca}^{2+}/\text{CaM}$ threshold may depend on the number of directions by which subunits can autophosphorylate their neighbors. Note that in the results up to this point, autophosphorylation was limited to occurring in a single direction, or degree of freedom. That is, subunits could only autophosphorylate their adjacent neighbors in a counter-clockwise fashion [17, 56, 57]. We therefore created alternative versions of our model in which autophosphorylation could occur with multiple degrees of freedom: two degrees of freedom in which intra-ring phosphorylation occurs in counter- and clock-wise directions, and three degrees of freedom in which both intra-ring and trans-ring phosphorylation occurs. We used these higher-degree of freedom models to monitor the rates of pThr-286 formation both in bulk and on an individual subunit basis. As expected, pThr-286 formation and intra-holoenzyme propagation rates increased with increasing degrees of freedom (see S1 Appendix, Figure S5-S7), though the differences would likely not be distinguishable by bench-top experimentation. In addition, the length of time in which consecutive neighboring subunits remained autophosphorylated also increased with increasing degrees of freedom (S1 Appendix, Figure S7). This implied that subunits may be more frequently autophosphorylated on time-average with increasing degrees of freedom. We present this preliminary exploration of the implication of the degrees of freedom, or directionality of CaMKII holoenzyme autophosphorylation, in order to demonstrate various capabilities of the model. We note that current experimental techniques are not sensitive enough to be discriminated between the simulation results. More work needs to be done to better characterize the conditions or possibility of bidirectional autophosphorylation both experimentally and computationally. Future experimental and computational studies could perhaps explore the dependence of autophosphorylation on higher degrees of freedom.

CaM-dependent exclusion of PP1 binding stabilizes autophosphorylation

Figure 4 suggested a threshold of $\text{Ca}^{2+}/\text{CaM}$ activation beyond which CaMKII remains autophosphorylated, implying a balance between kinase and phosphatase activity. We wondered how a putative balance between CaMKII autophosphorylation and phosphatase activity might be regulated. In the previous experimental work by Urakubo *et al.*, maximally-phosphorylated CaMKII was maintained in the presence of PP1 and NMDAR peptide for as long as 8 hours (at 4°C). In that work, addition of the

kinase inhibitor K252a to phosphorylated CaMKII resulted in a steady decline in pThr-286 towards basal levels, suggesting that maintenance of pThr-286 over time was not due to low phosphatase activity, but rather a recovery of de-phosphorylated subunits back to a phosphorylated state. To recreate inhibition of kinase activity in our model, at time $t=30$ sec we introduced a high concentration (18.2 μM) of K252a, enough to bind all CaMKII subunits in the model. K252a binding results in a blocked CaMKII state that cannot be autophosphorylated (see Flag 2 in S1 Appendix). Importantly, the blocked CaMKII subunit can still be de-phosphorylated at pThr-286. In separate simulations we explored the effects of a phosphatase inhibitor, which was also introduced at $t=30$ sec. To simulate the introduction of a phosphatase inhibitor, we defined the catalytic rate of de-phosphorylation by PP1 ($k_{\text{cat}}^{\text{PP1}}$) as a time-dependent variable that assumed a value of zero at $t = 30$ sec. This implementation of kinase and phosphatase inhibition preserved normal CaM and PP1 binding dynamics.

In these simulations the model was stimulated with 22.8 μM CaM₄ ($\text{Ca}^{2+}/\text{CaM}$) for 2sec and either no inhibition (control), kinase activity inhibition, or phosphatase inhibition was implemented at 30sec as described above (Fig 5). As expected, inhibiting phosphatase activity (green trace) caused kinase activity to dominate, resulting in a steady increase in pThr-286 compared to the control (black trace). Surprisingly, the kinase-inhibition (blue trace) showed little difference in pThr-286 concentration over time compared to the control. Instead of causing a greater reduction in pThr-286 over time due to phosphatase activity as was expected, inhibition of kinase activity resulted in almost no difference in pThr-286 levels even in the presence of phosphatase activity. We hypothesized that some other, non-enzymatic mechanism in our model was contributing to the maintenance of pThr-286.

Fig 5. Blocking kinase or phosphatase activity. Average concentration of pThr-286 CaMKII subunits over time. For all traces, the model is stimulated by a 2 sec pulse of $\text{Ca}^{2+}/\text{CaM}$. At time $t=30$ sec (arrowhead), either a kinase inhibitor (blue trace) or phosphatase inhibitor (green trace) is introduced. No inhibitor is introduced in the control (black trace). Each trace represents the average of $N=50$ executions.

In every simulation presented thus far, we assumed that CaM binding to the CaMKII regulatory domain sterically hinders PP binding to the regulatory domain, and vice-versa. This was implemented in

the model via a rule that requires a subunit be unbound by CaM in order for PP to bind. To test the role of these exclusions, we created a second version of our model in which PP binding would be allowed regardless of the presence of bound CaM₄, and CaM₄ binding would be allowed regardless of the presence of PP. In contrast to our original “exclusive” model, the “non-exclusive” model required only that a subunit be pThr-286 in order for PP binding to be allowable. In other words, the non-exclusive model allowed Ca²⁺/CaM and PP to bind CaMKII agnostically of each other. Aside from this rule adjustment, our exclusive and non-exclusive models utilized identical parameters (see S1 Appendix Table S1 and S2). As in Fig 5, we selected a Ca²⁺/CaM bolus time of 2 sec. Again, we monitored both CaMKII activation (Figs 6A and 6B) and pThr-286 (Figs 6C and 6D) over 120 seconds of simulated time. Critically, both the exclusive and non-exclusive models were examined with high (purple trace) and low (orange trace) association rate parameter values for PP binding to CaMKII. Increasing and decreasing the association rate of PP (k_{on}^{PP} is normally set to 3 $\mu\text{M}^{-1}\text{sec}^{-1}$) to CaMKII by one order of magnitude accounted for parameter uncertainty and provided a magnified view of the signaling effects of CaM-mediated exclusion of PP binding.

Fig 6. Comparison of Exclusive and Non-exclusive Models. For all traces, models are stimulated by a 2sec pulse of Ca²⁺/CaM. (A) Active CaMKII subunits over time in our exclusive model. (B) Active CaMKII subunits over time in our non-exclusive model. (C) pThr-286 subunits over time in our exclusive model. (D) pThr-286 subunits over time in our non-exclusive model. (A-D) The parameter value for the rate of PP association (k_{on}^{PP}) with CaMKII is either increased (purple traces) or decreased (orange traces) by one order of magnitude. (E) Extension of Fig 5 to include non-exclusive model results; the exclusive model results are also shown in Fig 5. At time t=30sec (arrows), either a kinase inhibitor (light blue trace) or phosphatase inhibitor (light green trace) is introduced. No inhibitor is introduced in the control (grey trace). All traces are the average of N=50 executions.

Our results suggested that CaM-dependent exclusion of PP is an important regulatory mechanism for maintaining CaMKII autophosphorylation levels. While the PP exclusion rule had little to no effect on the decay of CaMKII subunit de-activation (Fig 6A and Fig 6B, both decay constants -0.0004), pThr-286 (Fig 6C and Fig 6D) was highly influenced by the PP exclusion rule. In the exclusive model (Fig 6C), pThr-286 levels were steady and stable (decay constant -0.0004) despite varying the PP association rate parameter by two orders of magnitude. In contrast, the non-exclusive model (Fig 6D) showed that for a

high PP association rate, significant pThr-286 levels remained below 0.5 μM (Fig 6D low k_{on} trace has decay constant -0.006). Moreover, for a low PP association rate, the non-exclusive model attained lower pThr-286 levels compared to the exclusive model, and the pThr-286 levels then declined at a faster rate. We further emphasize the magnitudes of pThr-286 were noticeably influenced by the PP exclusion rule. Upon removing PP exclusion, peak magnitudes of pThr-286 were reduced from 3.2 μM (Fig 6C) to ~2.3 μM (Fig 6D). It seemed that in order to significantly activate and then maintain pThr-286 over longer time periods, CaMKII required a mechanism regulating phosphatase access, and a regulator of phosphatase access could be CaM itself.

To reinforce our assertion that CaM-dependent structural exclusion of PP binding stabilizes pThr-286, we repeated simulations shown in Fig 5, but with our non-exclusive model. In Fig 6E, we stimulated our non-exclusive model with a 2sec pulse of $\text{Ca}^{2+}/\text{CaM}$ and then monitored pThr-286 over time. For these simulations, $k_{\text{on}}^{\text{PP1}}$ was restored to its standard value of 3 $\mu\text{M}^{-1}\text{sec}^{-1}$. As in Fig 5, in separate simulations we inhibited at $t=30\text{sec}$ either phosphatase activity, kinase activity, or neither (control). The control (grey trace) was reminiscent of results in Fig 6D, in which pThr-286 was achieved but then slowly declined on a steady yet noisy basis. Notably, all non-exclusive model variants were much noisier than their exclusive model counterparts in Fig 6E. Inhibiting phosphatase activity (light green trace) in the non-exclusive model again caused kinase activity to dominate and pThr-286 levels to generally increase over time, similarly to the exclusive model. In contrast to the exclusive model, inhibiting kinase activity (light blue trace) in the non-exclusive model rapidly and totally abolished pThr-286. It seemed that for the non-exclusive model, in which CaM and PP could bind simultaneously, inhibiting kinase activity caused phosphatase activity to dominate. Taken together, these results suggested that in addition to supporting CaMKII subunit activation, CaM also has a role in maintaining CaMKII activity by blocking phosphatase access and thereby slowing down dephosphorylation.

CaM-dependent exclusion of PP1 binding may depend significantly on how we model $\text{Ca}^{2+}/\text{CaM}$. Until this point, we have modeled $\text{Ca}^{2+}/\text{CaM}$ as “2-state-2-step”, existing as either Ca^{2+} -unbound apo-

CaM or CaM₄ (2 states), which binds CaMKII in an initially- then fully-bound conformation (2 steps). However, previous experimental and computational studies have determined that sub-saturated Ca²⁺/CaM, with fewer than four Ca²⁺ bound, may significantly bind CaM-binding partners such as CaMKII [24, 47]. Indeed, Pepke *et al.* [24] and others use a “9-state-1-step” model of Ca²⁺/CaM, which explicitly accounts for each mode of Ca²⁺-binding at the CaM N- and C-termini. Importantly, each of the nine Ca²⁺/CaM states in the Pepke model has unique binding kinetics for CaMKII. We emphasize that these 9-state binding kinetics, which were measured using wild-type CaMKII *in vitro*, are incompatible with our 2-step CaM-binding model. In other words, a 9-state-2-step CaM-CaMKII model is difficult to parameterize because the available 9-state parameter values inherently account for 2-step CaM-binding. Moreover, the 9-state-2-step model would likely require a multi-state, rule-based model of CaM. And problematically, MCell 3.3 prohibits diffusion for rule-based species. Still, it is important to consider whether sub-saturated Ca²⁺/CaM states might still be able to structurally exclude, or out-compete, PP1-CaMKII binding.

Although a 9-state-2-step model of CaM-CaMKII binding is currently impractical, a 9-state-1-step model of CaM-CaMKII binding is practical, at least to explore how sub-saturated Ca²⁺/CaM could exclude PP1-CaMKII binding. For the 9-state-1-step model, we again use MCell 3.3 to describe the multi-state CaMKII holoenzyme, but we modify three of the flags described earlier in this paper. First, we remove the subunit docking and activation flags to reduce model noise and ensure the 9-state CaM-binding parameters remain appropriate. Second, we modify the CaM-binding flag to allow all nine Ca²⁺/CaM states (including apo-CaM) to bind CaMKII subunits. Thus, whereas in the 2-state-2-step CaMKII model subunit activation is defined by subunit opening, in the 9-state-1-step model activation is defined by CaM-binding. The parameters and reaction network for Ca²⁺-CaM binding and CaM-CaMKII binding may be found in Pepke *et al.* (see Figure 2C in [24]), and also refer to Table S3 in S1 Appendix. With our 9-state-1-step model (MCell code provided in the Purdue University Research Repository with DOI: 10.4231/MV0Z-8Z57, and parameters provided in S1 Appendix), we simulate using identical

conditions to those used for Fig 6A-6D, namely with 2000 Ca^{2+} (a CaM-saturating quantity, fully chelated at $t=2\text{sec}$), 450 CaM particles, and 30 CaMKII holoenzymes. Our 9-state-1-step model results are shown in Fig 7, where we again show that CaMKII subunit activation and pThr-286 levels are maintained on significantly longer timescales when CaM and PP cannot bind CaMKII simultaneously (Figs 7A and 7D). Compared to Fig 6, activation and pThr-286 levels are both higher and output noise is reduced, likely due to the absence of the activation flag and the fact that in a 9-state model, sub-saturated $\text{Ca}^{2+}/\text{CaM}$ significantly bind CaMKII and could contribute to its autophosphorylation. These may also explain the lack of difference in the peak magnitudes of pThr-286 in Figs 7C and 7F (compare to the peak magnitudes of Figs 6B and 6D). Specifically, for the 9-state-1-step model in Fig 7 maximal phosphorylation is achievable within 2 sec of Ca^{2+} stimulation, whereas 2 sec is not sufficient for maximal phosphorylation in the 2-state-2-step simulations (Fig 6). Finally, we observe that when only fully-saturated CaM_4 but no other $\text{Ca}^{2+}/\text{CaM}$ state is allowed to exclude PP (Figs 7B and 7E), model output is virtually identical to the fully non-exclusive case (Figs 7C and 7F). This suggests that sub-saturated $\text{Ca}^{2+}/\text{CaM}$ states may significantly contribute to PP1 exclusion. Indeed, this may be unsurprising given the affinity of states such as CaM_{2C} for CaMKII ($7.4\mu\text{M}$), which is only one order of magnitude larger than that of PP1 for CaMKII ($0.166\mu\text{M}$). Critically, though, in our 9-state-1-step model the CaM_{2C} -CaMKII affinity increases by 1000-fold when a CaMKII subunit is pThr-286, because we explicitly account for CaM-trapping [73]. Therefore, sub-saturated $\text{Ca}^{2+}/\text{CaM}$ states are very likely to out-compete PP1 and prevent its binding to CaMKII, at least from a kinetics perspective.

Fig 7. Exclusion in a 9-state-1-step CaM-CaMKII model. For all traces, models are stimulated by a 2sec pulse of Ca^{2+} . (A-C) Active CaMKII subunits over time in our 9-state-1-step model. (D-F) pThr-286 subunits over time. The parameter value for the rate of PP association ($k_{\text{on}}^{\text{PP1}}$) with CaMKII is either increased (purple traces) or decreased (orange traces) by one order of magnitude. Because this model version has inherently less output noise, all traces are the average of $N=20$ executions.

Discussion

In this work, we use rule- and particle-based methods with the software MCell to model the complete CaMKII holoenzyme. Rule-based modeling allows us to account for and monitor multiple

CaMKII states simultaneously without eliciting combinatorial explosion. By explicitly accounting for multiple CaMKII states, we can use this model to explore regulatory mechanisms such as the CaM-dependent maintenance of pThr-286 by structural exclusion of phosphatase binding to CaMKII.

Previous multi-state models of CaMKII exist but are different in focus and in scope from the present model. For example, our model is based on an earlier multi-state model by Stefan *et al.* (2012) [31] implemented in the particle-based stochastic simulator StochSim [74]. StochSim accounts for subunit topology (i.e. the user can specify whether a subunit is adjacent to another, and reactions can be neighbor-sensitive), but StochSim does not explicitly account for spatial information. MCell, as a spatial simulator, offers more possibilities to precisely account for spatial effects and to situate models in spatially realistic representations of cellular compartments. In addition, the model by Stefan *et al.* provides only for interactions between adjacent CaMKII molecules on the same hexamer ring and therefore models CaMKII as a hexamer, not a dodecamer. Similarly, another previous model of CaMKII by Michalski and Loew (2012) uses the softwares BioNetGen and VCell to offer an infinite subunit holoenzyme approximation (ISHA) of the CaMKII hexamer [75-77]. The ISHA asserts that under certain enzymatic assumptions, the output of a multi-state CaMKII model is independent of holoenzyme size when the number of subunits exceeds six. However, Michalski's ISHA model is most suitable for systems containing only one holoenzyme structure-dependent reaction such as the autophosphorylation at Thr-286. Additional reactions to describe actin binding [78] or subunit exchange [14, 15] may invalidate Michalski's ISHA, whereas our model can in the future readily accommodate additional, holoenzyme structure-dependent phenomena. Finally, a more recent rule-based model of the CaMKII holoenzyme by Li and Holmes [26] offers a detailed representation of how CaM binds to Ca^{2+} and subsequently activates CaMKII subunits, based on earlier results of CaM regulation [79]. Li and Holmes offer valuable and detailed insight into how CaM binding to CaMKII depends on Ca^{2+} dynamics. While our model is less detailed in representing the regulation of CaM itself, our model is much more detailed in representing other aspects of CaMKII regulation, including multiple modes of CaM binding, conformational change,

detailed holoenzyme structure, multiple phosphorylation sites, and dephosphorylation. We can in the future expand our MCell model to account for multiple holoenzyme structure-dependent phenomena and simultaneously incorporate this model into the broader Ca^{2+} -dependent signaling network.

This work in-part demonstrates the value of MCell as a rule-based modeling framework. Rule-based modeling accommodates much larger state spaces than is possible using conventional systems of differential equations. Admittedly, not all models (including models of CaMKII) require extensive state spaces, but rule-based modeling results can help justify the assumptions typically used to reduce a state space. For example, our model conditions yield, as shown in Fig 3A, negligible levels of initially-bound CaM compared to other states such as fully-bound CaM or pThr-286. Therefore, it might sometimes be appropriate to exclude an initially-bound CaM state from future implementations in frameworks for which combinatorial explosion is a concern. Aside from addressing combinatorial explosion, rule-based models are especially well-suited to discern otherwise concealed mechanisms, as exemplified by Di Camillo *et al.* who used rule-based models to identify a robustness-lending negative feedback mechanism in the insulin signaling pathway [49]. Furthermore, MCell describes CaMKII holoenzymes as discrete particles in space, which will lend realism to future spatial-stochastic models of Ca^{2+} -dependent signaling networks in the dendritic spine, a compartment in which the Law of Mass Action is invalid [24]. This particle-based framework also allows for individual subunit monitoring, which works in conjunction with the Blender software plugin, CellBlender (see S1 Movie).

One of the results of this work is the identification of distinct levels of CaMKII activation and pThr-286 in response to distinct pulses of Ca^{2+} /CaM stimulation. Distinct levels of CaMKII activation could tune the selectivity of CaMKII for certain downstream binding targets such as AMPA receptors or the structural protein PSD-95. If stimulation-dependent tuning of CaMKII activation were observed, it would be reminiscent of other studies that have implicated feedback loops [29] and binding dynamics [24] as regulators of Ca^{2+} -dependent enzyme activation. For example, a recent study suggests that competition is an emergent property that tunes the Ca^{2+} frequency dependence of CaM binding to

downstream targets, leading $\text{Ca}^{2+}/\text{CaM}$ to set distinct levels of calcineurin- and CaMKII-binding [12]. Similarly, CaMKII itself could preferentially select downstream binding partners as a function of its level of activation by $\text{Ca}^{2+}/\text{CaM}$, possibly providing a mechanism by which CaMKII facilitates certain LTP-related molecular events. Additionally, our observation of distinct levels of CaMKII activation and thresholded pThr-286 could be an indication of long-hypothesized switch-like behavior in synaptic plasticity [4, 70]. If switch-like behavior in fact occurs, then pThr-286 is likely maintained by a balance in kinase and phosphatase activity.

While investigating a putative interplay in CaMKII kinase and PP phosphatase activity in maintaining pThr-286 levels, we may have identified a CaM-dependent mechanism that blocks PP binding to CaMKII. In a model that excludes simultaneous binding of CaM and PP to CaMKII, pThr-286 significantly increases upon phosphatase inhibition, yet in the same model kinase inhibition causes little change in pThr-286 over time (Fig 5). In contrast, a non-exclusive model that allows simultaneous binding of CaM and PP shows that introduction of a kinase inhibitor rapidly abolishes pThr-286. These results suggest that CaM-dependent exclusion of PP may provide a stabilizing mechanism. Additionally, we use our MCell-based implementation of the model to monitor transitions between multiple states of distinct subunits within holoenzymes (Fig 7 and S1 Movie).

Fig 8. Visualizing Individual Subunits with MCell and CellBlender. In the exclusive model, PP does not bind a pThr-286 subunit until $\text{Ca}^{2+}/\text{CaM}$ dissociation (see $t = 85$ sec, comparing rows B and C). Each frame depicts the same CaMKII holoenzyme, from the same perspective, at identical time points under 50Hz $\text{Ca}^{2+}/\text{CaM}$ stimulation. Each dodecahedron is a single CaMKII subunit. (A) Inactive CaMKII subunits (white) spontaneously become active (black) and remain active while bound to $\text{Ca}^{2+}/\text{CaM}$. (B) Un-bound CaMKII subunits (yellow) will not bind $\text{Ca}^{2+}/\text{CaM}$ (red) and become $\text{Ca}^{2+}/\text{CaM}$ -bound (purple) unless the subunit had previously activated. (C) uThr-286 subunits (green) become pThr-286 (blue). If $\text{Ca}^{2+}/\text{CaM}$ dissociates from a pThr-286 subunit, then PP can bind and form a PP-CaMKII complex (cyan).

The major advance of this paper is to present a model of the regulation of 12-subunit CaMKII holoenzyme and its regulation by $\text{Ca}^{2+}/\text{CaM}$ and protein phosphatase. We assert that CaM-dependent exclusion of PP could provide a functional role for so-called “CaM trapping” [56] and possibly contribute to CaMKII bistability. Indeed, a model by Zhabotinsky (2000) explored CaMKII bistability, indicating

that two stable states of pThr-286 would in-part require very high CaMKII concentrations, seemingly to bolster kinase activity in the system [46]. However, the Zhabotinsky model assumes that CaM and PP1 could bind CaMKII simultaneously, possibly exaggerating the ability of PP1 to de-phosphorylate at Thr-286. If PP1 binding were to be encumbered in the Zhabotinsky model, perhaps through CaM-dependent exclusion, then bistability might be achievable at lower CaMKII concentrations.

Previous studies have sought to explore the dependence of CaMKII de-phosphorylation on the presence of Ca^{2+} /CaM. An experiment by Bradshaw *et al.* (2003) quantifies PP1-mediated de-phosphorylation rates of pThr-286 *in vitro*, in the presence or absence of free Ca^{2+} (see Figure 4B in [80]). In both the presence and absence of free Ca^{2+} at 0°C , Bradshaw *et al.* observe that pThr-286 levels decrease over 30 min at similar rates, in conditions with limiting ATP such that CaMKII cannot re-phosphorylate. These results could be interpreted to suggest that PP1 activity is independent of Ca^{2+} and in turn Ca^{2+} /CaM-binding to CaMKII. Note that in the Bradshaw results, regardless of the presence of free Ca^{2+} , CaMKII activation persists for at least tens of minutes. The persistence of CaMKII activity on relatively long timescales, even in the presence of phosphatase, is consistent with separate experimental results [22, 57, 59, 70, 73]. Our results suggest an alternative interpretation of these and Bradshaw's results. In our model, CaMKII activity persists for many minutes only when CaM excludes PP1. Indeed, the effect of CaM exclusion on the timescale of CaMKII activation is even more pronounced in our 9-state-1-step CaM-binding model results.

Our 9-state-1-step model suggests that following termination of Ca^{2+} flux, sub-saturated Ca^{2+} /CaM states may significantly contribute to PP1-exclusion (S1 Appendix). First, this agreement between our 9-state-1-step and primary 2-state-2-step models is a testament to the model's robustness to uncertainty with parameterizing the docking and activation flags. Further, our 9-state-1-step results are also consistent with Bradshaw's results, as seen in Figure 9 of that paper (their supplementary material). Specifically, Bradshaw *et al.* explore in their supplement how CaMKII autophosphorylation levels equilibrate in the presence of various Ca^{2+} concentrations. Importantly, many of the Ca^{2+} concentrations

are at levels that would not saturate CaM. Nonetheless, with sub-saturated $\text{Ca}^{2+}/\text{CaM}$ significant levels of CaMKII autophosphorylation are maintained even by 7.5 hours of incubation, even in the presence of PP1, indicating that sub-saturated $\text{Ca}^{2+}/\text{CaM}$ states could be playing a key role in maintenance of CaMKII autophosphorylation. In S1 Appendix, we show that the $\text{Ca}^{2+}/\text{CaM}$ state predominantly responsible for PP1-exclusion following termination of Ca^{2+} stimulation in the 9-state-1-step model is apo-CaM. Apo-CaM remaining bound to CaMKII is consistent with results by Brown *et al.*, who determine that when free Ca^{2+} levels decrease, Ca^{2+} dissociates from CaM before CaM dissociates from its binding partner [81]. Of course, the affinity of apo-CaM for CaMKII (1.45mM) should be insufficient to out-compete PP1-CaMKII binding (0.16 μM). Yet because the 9-state-1-step model explicitly accounts for CaM-trapping by increasing the affinity of pThr-286 subunits for $\text{Ca}^{2+}/\text{CaM}$ by 1000-fold [73], the affinity of pThr-286 CaMKII for apo-CaM (1.45 μM) is within one order of magnitude as that of PP1 (0.16 μM). (In the original 2-state-2-step model, we provide for CaM-trapping implicitly through the 2-step CaM-binding.) Thus, apo-CaM may be able to compete with PP1 for CaMKII-binding, but it now remains for future experimental studies to directly quantify the kinetics and/or structure of the apo-CaM interaction with pThr-286 CaMKII. Determining the effect of CaM-trapping on sub-saturated $\text{Ca}^{2+}/\text{CaM}$ states is outside the scope of the current work. Notably, during dynamic Ca^{2+} flux (S1 Appendix), we observe that non-apo- $\text{Ca}^{2+}/\text{CaM}$ states such as $\text{CaM}_{2\text{C}}$ may contribute to maintenance of pThr-286. This indicates that even if structural studies reveal that apo-CaM is insufficient to out-compete PP1, it is possible that CaM-dependent PP1 exclusion could contribute at least somewhat to pThr-286 acquisition and maintenance during Ca^{2+} stimulation. Clearly, further structural and kinetic studies of the CaM-CaMKII and PP1-CaMKII interaction are needed.

CaM-dependent PP exclusion could provide an added layer of robustness to similar mechanisms that may protect pThr-286 from de-phosphorylation. For example, Mullasseril *et al.* (2007) observe that endogenous, PSD-resident PP1 cannot de-phosphorylate CaMKII at pThr-286, whereas adding exogenous PP1 does cause de-phosphorylation [71]. The results by Mullasseril *et al.* suggest that endogenous PP1 is

somehow sequestered by the PSD scaffold, and only upon saturation of this scaffold by exogenous PP1 does pThr-286 become de-phosphorylated. Our results indicate that perhaps in addition to saturating the PSD scaffold, the added exogenous PP1 could be out-competing CaM for binding to CaMKII, thereby terminating protection of pThr-286 by CaM. As another example, Urakubo *et al.* suggest that pThr-286 could be protected from PP activity by GluN2B binding, showing that GluN2B peptides are necessary for an apparent CaMKII bistability *in vitro* [72]. Notably, Urakubo *et al.*, when using equal concentrations of CaM and CaMKII subunits, observe a slow and steady decline in pThr-286 upon kinase inhibition that has a similar rate as that seen in the Bradshaw study [80], taking place over the course of hours, which we only observe in our exclusive model. Urakubo *et al.* also mention that when basal levels of Ca^{2+} are set below 0.2 μM , CaMKII autophosphorylation decreases to basal levels within 6 hours, perhaps indicating that GluN2B-dependent exclusion of PP1 is necessary but not sufficient for maintaining pThr-286 levels; sufficiently high levels of $\text{Ca}^{2+}/\text{CaM}$ may also be required. Overall, it seems scaffold-dependent sequestration of PP1 [71], GluN2B-dependent PP exclusion [72], and CaM-dependent PP exclusion could together provide considerable robustness of pThr-286 to phosphatase activity.

Methods

Simulation Methods

In each MCell execution, proteins are instantiated at time zero having random positions within a 0.0328 μm^3 (0.0328 fL) cube, with each edge being 0.32 μm in length. All proteins are described as three-dimensional volume molecules having the following concentrations: 1.52 μM CaMKII (30 holoenzymes, 18.24 μM and 360 individual CaMKII subunits), 22.8 μM CaM (450 discrete proteins), and 0.86 μM PP1 (17 discrete proteins). Because CaMKII particles are modeled using the specialized COMPLEX_MOLECULE syntax and MCell 3.3 does not accommodate diffusion for such particles, CaMKII is given no diffusion constant. In contrast, CaM and PP1 are simple volume-type molecules that move about the model space with a diffusion constant $6 \times 10^{-6} \text{ cm}^2/\text{sec}$, so chosen to minimize the effects of any possible spatial localizations that may arise during a simulation. We emphasize that because this model does not explore spatial effects and, indeed, does not utilize a physiological spine geometry, using

such a relatively fast diffusion parameter ensures that spatial effects do not confound our results. Future models exploring the spatial dependence of CaMKII holoenzyme activity in the dendritic spine may choose to adopt different diffusion parameters. All models are run at a time step of 0.1 μ s for a total of either 20 or 120 seconds of simulation time, depending on the model variant.

MCell is a particle-based spatial-stochastic simulation engine. In a particle-based framework, individual protein species are modeled as discrete objects in space, rather than bulk/well-mixed fluids. At each model timestep, MCell calculates each protein particle's subsequent diffusion distance and trajectory, in addition to the particle's probabilities for reacting with any nearby particles. More information about MCell's internal algorithms may be found at mcell.org and in publications such as those by Bartol *et al.* [51]. In short, the particle-based framework in MCell provides for spatial and stochastic considerations because each protein particle has unique spatial coordinates that proceed along random (stochastic) trajectories. Importantly, we assert that spatial-stochastic frameworks may be essential to characterizing CaMKII regulation, because 1) proteins in the spine are spatially organized and 2) protein copy numbers in the spine are low (tens to hundreds each), possibly invalidating the Law of Mass Action. Because MCell models are stochastic and change with each simulation, we average the output of many identical simulations. To ensure that the averaged output converges and is statistically significant, all model variants are repeated 50 times each.

CaM activation/inactivation is modeled by a pair of forcing functions which serve as a proxy for Ca^{2+} flux. Both forcing functions are time-dependent square waves and inform the rates at which free CaM transitions between states (see S1 Appendix; Figure S2) Equation 1 rapidly transitions all free CaM towards an active ($\text{Ca}^{2+}/\text{CaM}$) state, and Equation 2 rapidly transitions all free CaM towards an inactive (apo-CaM) state.

$$(1)F_{activation}(t) = \begin{cases} 100000000, & t = n_i \\ 0, & t \neq n_i \end{cases}$$

$$(2)F_{inactivation}(t) = \begin{cases} 0, t = n_i \\ 100000000, t \neq n_i \end{cases}$$

For both Equations 1 and 2, $n = i/f$ where i is the number of time step iterations and f is frequency. Time t iterates at 0.01sec intervals for the complete duration of a simulation. Equations 1 and 2 therefore yield a peak width of 0.01sec regardless of frequency, which allows us to directly compare the effect of different $\text{Ca}^{2+}/\text{CaM}$ frequencies on CaMKII activity, without having to account for variable amounts of $\text{Ca}^{2+}/\text{CaM}$ exposure per pulse. In separate simulations without frequency dependence (i.e. $\text{Ca}^{2+}/\text{CaM}$ is continuously available to CaMKII), Equation 1 is adjusted to always fulfill the $t=n_i$ condition. Similarly, for pulse simulations in which $\text{Ca}^{2+}/\text{CaM}$ becomes withdrawn or blocked, Equations 1 and 2 are given abbreviated time domains.

All MCell code and associated files are available online at Github, the Purdue University Research Repository, and the University of Edinburgh Repository. Material will be made available upon publication.

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References

1. Erondy NE, Kennedy MB. Regional distribution of type-II Ca^{2+} calmodulin-dependent protein-kinase in rat-brain. *J Neurosci.* 1985;5(12):3270-7.
2. Kennedy MB. Regulation of synaptic transmission in the central nervous-system - long-term potentiation. *Cell.* 1989;59(5):777-87. doi: 10.1016/0092-8674(89)90601-6.
3. Silva AJ, Stevens CF, Tonegawa S, Wang YY. Deficient hippocampal long-term potentiation in alpha-calcium-calmodulin kinase-II mutant mice. *Science.* 1992;257(5067):201-6. doi: 10.1126/science.1378648.
4. Lisman J, Schulman H, Cline H. The molecular basis of CaMKII function in synaptic and behavioural memory. *Nat Rev Neurosci.* 2002;3(3):175-90. doi: 10.1038/nrn753.
5. Kennedy MB. Synaptic signaling in learning and memory. *Cold Spring Harbor Perspect Biol.* 2013;8. doi: 10.1101/cshperspect.a016824.
6. Harris KM. Structure, development, and plasticity of dendritic spines. *Curr Opin Neurobiol.* 1999;9(3):343-8. doi: 10.1016/s0959-4388(99)80050-6.
7. Evans RC, Morera-Herreras T, Cui YH, Du K, Sheehan T, Kotaleski JH, et al. The effects of NMDA subunit composition on calcium influx and spike timing-dependent plasticity in striatal medium spiny neurons. *PLoS Comput Biol.* 2012;8(4):13. doi: 10.1371/journal.pcbi.1002493.
8. Kennedy MB. Synaptic signaling in learning and memory. *Cold Spring Harbor Perspect Biol.* 2016;8(2):16. doi: 10.1101/cshperspect.a016824.

10. He Y, Kulasiri D, Samarasinghe S. Systems biology of synaptic plasticity: A review on N-methyl-D-aspartate receptor mediated biochemical pathways and related mathematical models. *Biosystems*. 2014;122:7-18. doi: 10.1016/j.biosystems.2014.06.005.
11. Xia ZG, Storm DR. The role of calmodulin as a signal integrator for synaptic plasticity. *Nat Rev Neurosci*. 2005;6(4):267-76. doi: 10.1038/nrn1647.
12. Romano DR, Pharris MC, Patel NM, Kinzer-Ursem TL. Competitive tuning: Competition's role in setting the frequency-dependence of Ca²⁺-dependent proteins. *PLoS Comput Biol*. 2017;13(11):26. doi: 10.1371/journal.pcbi.1005820.
13. Bennett MK, Erondur NE, Kennedy MB. Purification and characterization of a calmodulin-dependent protein-kinase that is highly concentrated in brain. *J Biol Chem*. 1983;258(20):2735-44.
14. Stratton M, Lee IH, Bhattacharyya M, Christensen SM, Chao LH, Schulman H, et al. Activation-triggered subunit exchange between CaMKII holoenzymes facilitates the spread of kinase activity. *eLife*. 2014;3:28. doi: 10.7554/eLife.01610.
15. Bhattacharyya M, Stratton MM, Going CC, McSpadden ED, Huang Y, Susa AC, et al. Molecular mechanism of activation-triggered subunit exchange in Ca²⁺/calmodulin-dependent protein kinase II. *eLife*. 2016;5:32. doi: 10.7554/eLife.13045.
16. Rosenberg OS, Deindl S, Sung RJ, Nairn AC, Kuriyan J. Structure of the autoinhibited kinase domain of CaMKII and SAXS analysis of the holoenzyme. *Cell*. 2005;123(5):849-60. doi: 10.1016/j.cell.2005.10.029.
17. Chao LH, Stratton MM, Lee IH, Rosenberg OS, Levitz J, Mandell DJ, et al. A mechanism for tunable autoinhibition in the structure of a human ca²⁺/calmodulin-dependent kinase II holoenzyme. *Cell*. 2011;146(5):732-45. doi: 10.1016/j.cell.2011.07.038.
18. Myers JB, Zaegel V, Coultrap SJ, Miller AP, Bayer KU, Reichow SL. The CaMKII holoenzyme structure in activation-competent conformations. *Nat Commun*. 2017;8:14. doi: 10.1038/ncomms15742.
19. Hoffman L, Stein RA, Colbran RJ, McHaourab HS. Conformational changes underlying calcium/calmodulin-dependent protein kinase II activation. *Embo J*. 2011;30(7):1251-62. doi: 10.1038/emboj.2011.40.
20. Giese KP, Fedorov NB, Filipkowski RK, Silva AJ. Autophosphorylation at Thr(286) of the alpha calcium-calmodulin kinase II in LTP and learning. *Science*. 1998;279(5352):870-3. doi: 10.1126/science.279.5352.870.
21. Colbran RJ, Fong YL, Schworer CM, Soderling TR. Regulatory interactions of the calmodulin-binding, inhibitory, and autophosphorylation domains of Ca²⁺/calmodulin-dependent protein kinase-II. *Journal of Biological Chemistry*. 1988;263(34):18145-51.
22. Miller SG, Kennedy MB. Regulation of brain type-II Ca-2+ calmodulin-dependent protein-kinase by autophosphorylation - a Ca-2+-triggered molecular switch. *Cell*. 1986;44(6):861-70. doi: 10.1016/0092-8674(86)90008-5.
23. Hudmon A, Schulman H. Neuronal Ca²⁺/calmodulin-dependent protein kinase II: The role of structure and autoregulation in cellular function. *Ann Rev Biochem*. 2002;71:473-510. doi: 10.1146/annurev.biochem.71.110601.135410.
24. Pepke S, Kinzer-Ursem T, Mihalas S, Kennedy MB. A dynamic model of interactions of Ca²⁺, calmodulin, and catalytic subunits of ca²⁺/calmodulin-dependent protein kinase II. *PLoS Comput Biol*. 2010;6(2):15. doi: 10.1371/journal.pcbi.1000675.
25. Li Y, Holmes WR. Comparison of CaMKinase II activation in a dendritic spine computed with deterministic and stochastic models of the NMDA synaptic conductance. *Neurocomputing*. 2000;32:1-7. doi: 10.1016/s0925-2312(00)00137-5.
26. Li X, Holmes WR. Biophysical attributes that affect CaMKII activation deduced with a novel spatial stochastic simulation approach. *PLOS Computational Biology*; 2018.
27. Holmes WR. Models of calmodulin trapping and CaM kinase II activation in a dendritic spine. *J Comput Neurosci*. 2000;8(1):65-85. doi: 10.1023/a:1008969032563.
28. Zeng SY, Holmes WR. The effect of noise on CaMKII activation in a dendritic spine during LTP induction. *J Neurophysiol*. 2010;103(4):1798-808. doi: 10.1152/jn.91235.2008.

29. Hayer A, Bhalla US. Molecular switches at the synapse emerge from receptor and kinase traffic. *PLoS Comput Biol*. 2005;1(2):137-54. doi: 10.1371/journal.pcbi.0010020.
30. Keller DX, Franks KM, Bartol TM, Sejnowski TJ. Calmodulin activation by calcium transients in the postsynaptic density of dendritic spines. *PLoS One*. 2008;3(4):16. doi: 10.1371/journal.pone.0002045.
31. Stefan MI, Marshall DP, Le Novère N. Structural analysis and stochastic modelling suggest a mechanism for calmodulin trapping by CaMKII. *PLoS One*. 2012;7(1):14. doi: 10.1371/journal.pone.0029406.
32. Stefan MI, Bartol TM, Sejnowski TJ, Kennedy MB. Multi-state modeling of biomolecules. *PLoS Comput Biol*. 2014;10(9):9. doi: 10.1371/journal.pcbi.1003844.
33. Li L, Stefan MI, Le Novère N. Calcium input frequency, duration and amplitude differentially modulate the relative activation of calcineurin and CaMKII. *PLoS One*. 2012;7(9):17. doi: 10.1371/journal.pone.0043810.
34. Zhabotinsky AM, Camp RN, Epstein IR, Lisman JE. Role of the neurogranin concentrated in spines in the induction of long-term potentiation. *J Neurosci*. 2006;26(28):7337-47. doi: 10.1523/jneurosci.0729-06.2006.
35. Lucic V, Greif GJ, Kennedy MB. Detailed state model of CaMKII activation and autophosphorylation. *Eur Biophys J Biophys Lett*. 2008;38(1):83-98. doi: 10.1007/s00249-008-0362-4.
36. Byrne MJ, Waxham MN, Kubota Y. The impacts of geometry and binding on CaMKII diffusion and retention in dendritic spines. *J Comput Neurosci*. 2011;31(1):1-12. doi: 10.1007/s10827-010-0293-9.
37. Johnson T, Bartol T, Sejnowski T, Mjolsness E. Model reduction for stochastic CaMKII reaction kinetics in synapses by graph-constrained correlation dynamics. *Phys Biol*. 2015;12(4):16. doi: 10.1088/1478-3975/12/4/045005.
38. Chylek LA, Harris LA, Tung CS, Faeder JR, Lopez CF, Hlavacek WS. Rule-based modeling: a computational approach for studying biomolecular site dynamics in cell signaling systems. *Wiley Interdiscip Rev-Syst Biol*. 2014;6(1):13-36. doi: 10.1002/wsbm.1245.
39. Sejnowski TJ, Poggio T. Computational modeling methods for neuroscientists foreword. In: DeSchutter E, editor. *Computational Modeling Methods for Neuroscientists*. Computational Neuroscience-MIT. Cambridge: Mit Press; 2009. p. VII-+.
40. Blinov ML, Faeder JR, Goldstein B, Hlavacek WS. BioNetGen: software for rule-based modeling of signal transduction based on the interactions of molecular domains. *Bioinformatics*. 2004;20(17):3289-91. doi: 10.1093/bioinformatics/bth378.
41. Sneddon MW, Faeder JR, Emonet T. Efficient modeling, simulation and coarse-graining of biological complexity with NFsim. *Nat Methods*. 2011;8(2):177-U12. doi: 10.1038/nmeth.1546.
42. Bartol TM, Keller DX, Kinney JP, Bajaj CL, Harris KM, Sejnowski TJ, et al. Computational reconstitution of spine calcium transients from individual proteins. *Frontiers in synaptic neuroscience*. 2015;7:17. doi: 10.3389/fnsyn.2015.00017.
43. Strack S, Barban MA, Wadzinski BE, Colbran RJ. Differential inactivation of postsynaptic density-associated and soluble Ca²⁺/calmodulin-dependent protein kinase II by protein phosphatases 1 and 2A. *Journal of Neurochemistry*. 1997;68(5):2119-28.
44. Strack S, Kini S, Ebner FF, Wadzinski BE, Colbran RJ. Differential cellular and subcellular localization of protein phosphatase 1 isoforms in brain. *J Comp Neurol*. 1999;413(3):373-84.
45. Schworer CM, Colbran RJ, Soderling TR. Reversible generation of a Ca²⁺-independent form of Ca²⁺(calmodulin)-dependent protein kinase-II by an autophosphorylation mechanism. *J Biol Chem*. 1986;261(19):8581-4.
46. Zhabotinsky AM. Bistability in the Ca²⁺/calmodulin-dependent protein kinase-phosphatase system. *Biophys J*. 2000;79(5):2211-21. doi: 10.1016/s0006-3495(00)76469-1.
47. Shifman JM, Choi MH, Mihalas S, Mayo SL, Kennedy MB. Ca²⁺/calmodulin-dependent protein kinase II (CaMKII) is activated by calmodulin with two bound calciums. *Proc Natl Acad Sci U S A*. 2006;103(38):13968-73. doi: 10.1073/pnas.0606433103.
48. Blackwell KT. Approaches and tools for modeling signaling pathways and calcium dynamics in neurons. *J Neurosci Methods*. 2013;220(2):131-40. doi: 10.1016/j.jneumeth.2013.05.008.

49. Forest A, Swulius MT, Tse JKY, Bradshaw JM, Gaertner T, Waxham MN. Role of the N- and C-lobes of calmodulin in the activation of Ca(2+)/calmodulin-dependent protein kinase II. *Biochemistry*. 2008;47(40):10587-99. doi: 10.1021/bi8007033.
50. Lisman JE, Zhabotinsky AM. A model of synaptic memory: A CaMKII/PP1 switch that potentiates transmission by organizing an AMPA receptor anchoring assembly. *Neuron*. 2001;31(2):191-201. doi: 10.1016/s0896-6273(01)00364-6.
51. Bartol T, Derkach M, Faeder J. *MCCell. Encyclopedia of computational neuroscience*; 2015. p. 1673-76.
52. Torok K, Tzortzopoulos A, Grabarek Z, Best SL, Thorogate R. Dual effect of ATP in the activation mechanism of brain Ca2+/calmodulin-dependent protein kinase II by Ca2+/calmodulin. *Biochemistry*. 2001;40(49):14878-90. doi: 10.1021/bi010920+.
53. Tzortzopoulos A, Torok K. Mechanism of the T286A-mutant alpha CaMKII interactions with Ca2+/calmodulin and ATP. *Biochemistry*. 2004;43(21):6404-14. doi: 10.1021/bi036224m.
54. Hoffman L, Chandrasekar A, Wang X, Putkey JA, Waxham MN. Neurogranin alters the structure and calcium binding properties of calmodulin. *J Biol Chem*. 2014;289(21):14644-55. doi: 10.1074/jbc.M114.560656.
55. Tse JKY, Giannetti AM, Bradshaw JM. Thermodynamics of calmodulin trapping by Ca2+/calmodulin-dependent protein kinase II: Subpicomolar K-d determined using competition titration calorimetry. *Biochemistry*. 2007;46(13):4017-27. doi: 10.1021/bi700013y.
56. Hanson PI, Meyer T, Stryer L, Schulman H. Dual role of calmodulin in autophosphorylation of multifunctional CaM kinase may underlie decoding of calcium signals. *Neuron*. 1994;12(5):943-56. doi: 10.1016/0896-6273(94)90306-9.
57. Bradshaw JM, Hudmon A, Schulman H. Chemical quenched flow kinetic studies indicate an intraholoenzyme autophosphorylation mechanism for Ca2+/calmodulin-dependent protein kinase II. *J Biol Chem*. 2002;277(23):20991-8. doi: 10.1074/jbc.M202154200.
58. Shields SM, Ingebritsen TS, Kelly PT. Identification of protein phosphatase-1 in synaptic junctions - dephosphorylation of endogenous calmodulin-dependent kinase-II and synapse-enriched phosphoproteins. *J Neurosci*. 1985;5(12):3414-22.
59. Dosemeci A, Reese TS. Inhibition of endogenous phosphatase in a postsynaptic density fraction allows extensive phosphorylation of the major postsynaptic density protein. *J Neurochem*. 1993;61(2):550-5.
60. Waxham MN, Tsai AL, Putkey JA. A mechanism for calmodulin (CaM) trapping by CaM-kinase II defined by a family of CaM-binding peptides. *Journal of Biological Chemistry*. 1998;273(28):17579-84. doi: 10.1074/jbc.273.28.17579.
61. Meador WE, Means AR, Quirocho FA. Target enzyme recognition by calmodulin - 2.4-angstrom structure of a calmodulin-peptide complex. *Science*. 1992;257(5074):1251-5. doi: 10.1126/science.1519061.
62. Mulkey RM, Endo S, Shenolikar S, Malenka RC. Involvement of a calcineurin/inhibitor-1 phosphatase cascade in hippocampal long-term depression. *Nature*. 1994;369(6480):486-8. doi: 10.1038/369486a0.
63. Ragusa MJ, Dancheck B, Critton DA, Nairn AC, Page R, Peti W. Spinophilin directs protein phosphatase 1 specificity by blocking substrate binding sites. *Nat Struct Mol Biol*. 2010;17(4):459-U100. doi: 10.1038/nsmb.1786.
64. Kelker MS, Page R, Peti W. Crystal structures of protein phosphatase-1 bound to nodularin-r and tautomycin: a novel scaffold for structure-based drug design of serine/threonine phosphatase inhibitors. *J Mol Biol*. 2009;385(1):11-21. doi: 10.1016/j.jmb.2008.10.053.
65. Hsieh-Wilson LC, Allen PB, Watanabe T, Nairn AC, Greengard P. Characterization of the neuronal targeting protein spinophilin and its interactions with protein phosphatase-1. *Biochemistry*. 1999;38(14):4365-73. doi: 10.1021/bi982900m.

66. Payne ME, Fong YL, Ono T, Colbran RJ, Kemp BE, Soderling TR, et al. Calcium calmodulin-dependent protein kinase-ii - characterization of distinct calmodulin binding and inhibitory domains. *J Biol Chem.* 1988;263(15):7190-5.
67. Miller P, Zhabotinsky AM, Lisman JE, Wang XJ. The stability of a stochastic CaMKII switch: Dependence on the number of enzyme molecules and protein turnover. *PLoS Biol.* 2005;3(4):705-17. doi: 10.1371/journal.pbio.0030107.
68. Kolodziej SJ, Hudmon A, Waxham MN, Stoops JK. Three-dimensional reconstructions of calcium/calmodulin dependent (CaM) kinase II alpha and truncated CaM kinase II alpha reveal a unique organization for its structural core and functional domains. *J Biol Chem.* 2000;275(19):14354-9. doi: 10.1074/jbc.275.19.14354.
69. De Koninck P, Schulman H. Sensitivity of CaM kinase II to the frequency of Ca²⁺ oscillations. *Science.* 1998;279(5348):227-30. doi: 10.1126/science.279.5348.227.
70. Lisman JE. A mechanism for memory storage insensitive to molecular turnover - a bistable autophosphorylating kinase. *Proc Natl Acad Sci U S A.* 1985;82(9):3055-7. doi: 10.1073/pnas.82.9.3055.
71. Mullasseril P, Dosemeci A, Lisman JE, Griffith LC. A structural mechanism for maintaining the 'on-state' of the CaMKII memory switch in the post-synaptic density. *J Neurochem.* 2007;103(1):357-64. doi: 10.1111/j.1471-4159.2007.04744.x.
72. Urakubo H, Sato M, Ishii S, Kuroda S. In vitro reconstitution of a CaMKII memory switch by an nmda receptor-derived peptide. *Biophys J.* 2014;106(6):1414-20. doi: 10.1016/j.bpj.2014.01.026.
73. Meyer T, Hanson PI, Stryer L, Schulman H. Calmodulin trapping by calcium-calmodulin dependent protein-kinase. *Science.* 1992;256(5060):1199-202. doi: 10.1126/science.256.5060.1199.
74. Le Novère N, Shimizu TS. STOCHSIM: modelling of stochastic biomolecular processes. *Bioinformatics.* 2001;17(6):575-6. doi: 10.1093/bioinformatics/17.6.575.
75. Michalski PJ, Loew LM. CaMKII activation and dynamics are independent of the holoenzyme structure: an infinite subunit holoenzyme approximation. *Phys Biol.* 2012;9(3):13. doi: 10.1088/1478-3975/9/3/036010.
76. Slepchenko BM, Schaff JC, Macara I, Loew LM. Quantitative cell biology with the virtual cell. *Trends Cell Biol.* 2003;13(11):570-6. doi: 10.1016/j.tcb.2003.09.003.
77. Harris LA, Hogg JS, Tapia JJ, Sekar JAP, Gupta S, Korsunsky I, et al. BioNetGen 2.2: advances in rule-based modeling. *Bioinformatics.* 2016;32(21):3366-8. doi: 10.1093/bioinformatics/btw469.
78. Khan S, Conte I, Carter T, Bayer KU, Molloy JE. Multiple CaMKII binding modes to the actin cytoskeleton revealed by single-molecule imaging. *Biophys J.* 2016;111(2):395-408. doi: 10.1016/j.bpj.2016.06.007.
79. Linse S, Helmersson A, Forsen S. Calcium-binding to calmodulin and its globular domains. *J Biol Chem.* 1991;266(13):8050-4.
80. Bradshaw JM, Kubota Y, Meyer T, Schulman H. An ultrasensitive Ca²⁺/calmodulin-dependent protein kinase II-protein phosphatase 1 switch facilitates specificity in postsynaptic calcium signaling. *Proc Natl Acad Sci USA.* 2003;100(18):10512-7. doi: 10.1073/pnas.1932759100.
81. Brown SE, Martin SR, Bayley PM. Kinetic control of the dissociation pathway of calmodulin-peptide complexes. *J Biol Chem.* 1997;272(6):3389-97. doi: 10.1074/jbc.272.6.3389.

Supporting Information

S1 Appendix. Appendix. This document enumerates the model parameters, discusses combinatorial explosion, shows alternative visualizations of select data, and discusses the quantitative basis for PP1/CaM mutual exclusion from CaMKII binding.